

Thermodynamics

I. The Zeroth Law and Related Concepts

What Zeroth Law gives us...

- temperature and thermometers
- Why we know two systems are in thermal equilibrium even they never meet each other (through a third party or many thermometers working at different places)

Related Concepts

- System and surrounding, and how they interact (thermal contact, and more)
- Equilibrium (thermodynamic)
- State variables & State functions

Zeroth Law

If each of two systems is in thermal equilibrium with a third, then they are in thermal equilibrium with one another.

↑ This is the formal statement.

In plain language,

If systems A and B are at the same temperature, and B and C are at the same temperature, then A and C are at the same temperature.

i.e. when two systems are put into thermal contact (& wait for some time) and achieve equilibrium, they have one quantity (temperature) in common.

- Thermodynamics is based on daily life experience/observations
- No need to mention what are the stuff in the systems

- gases, liquids, solids ...

- Don't need to refer to atoms/molecules

this is statistical mechanics' job!

- Don't need to refer to microscopic models of matter

e.g. an array of atoms forming a solid with a Hamiltonian that carries quadratic (harmonic) and third order (anharmonic) terms

Make thermodynamics
work for macroscopic
systems of any kind!

→ systems with many stuff!

Einstein (1949)[†]:

"

... A theory is more impressive the greater the simplicity of its premises,
... Therefore, classical thermodynamics has made a deep impression on me.
It is the only physical theory of universal content which I am
convinced, ..., will never be overthrown."

[†] Holton and Elkana, "Albert Einstein, Historical and Cultural Perspectives", (Princeton Univ. Press)

Simple but deep!

- System + (what's not the system)

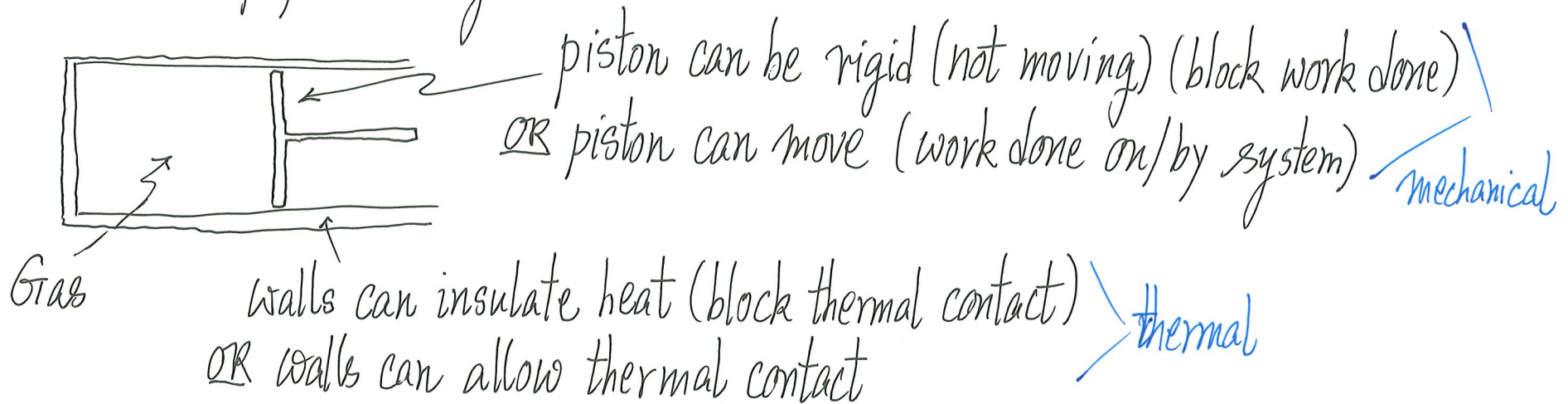
what we focus on

surrounding (could do something to affect the system)

- Add/Take something called "Heat"
- "Do work" on the system
- Add/Take matter to/from system

depends on nature of boundary

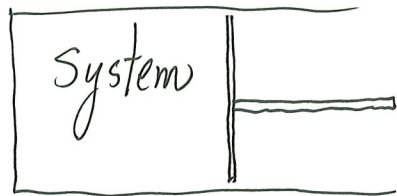
- A standard physicist's system



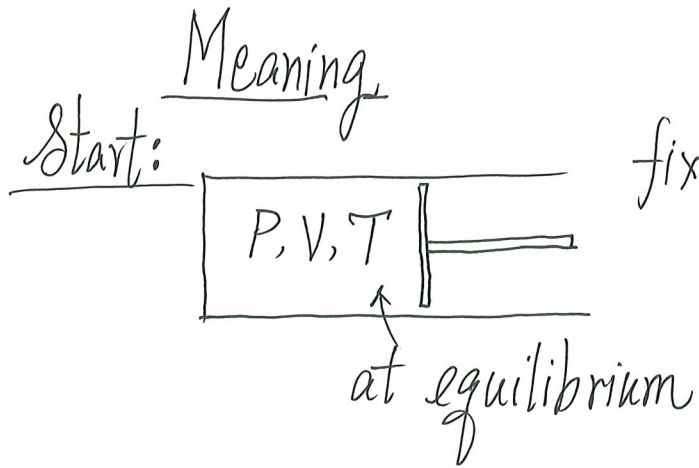
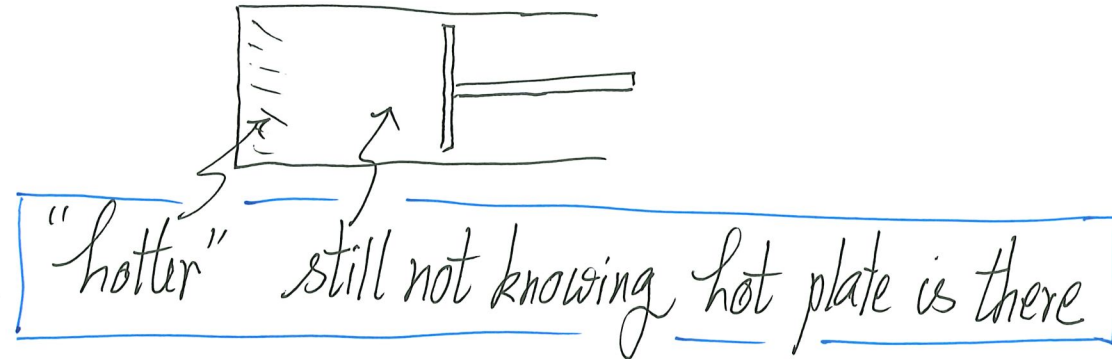
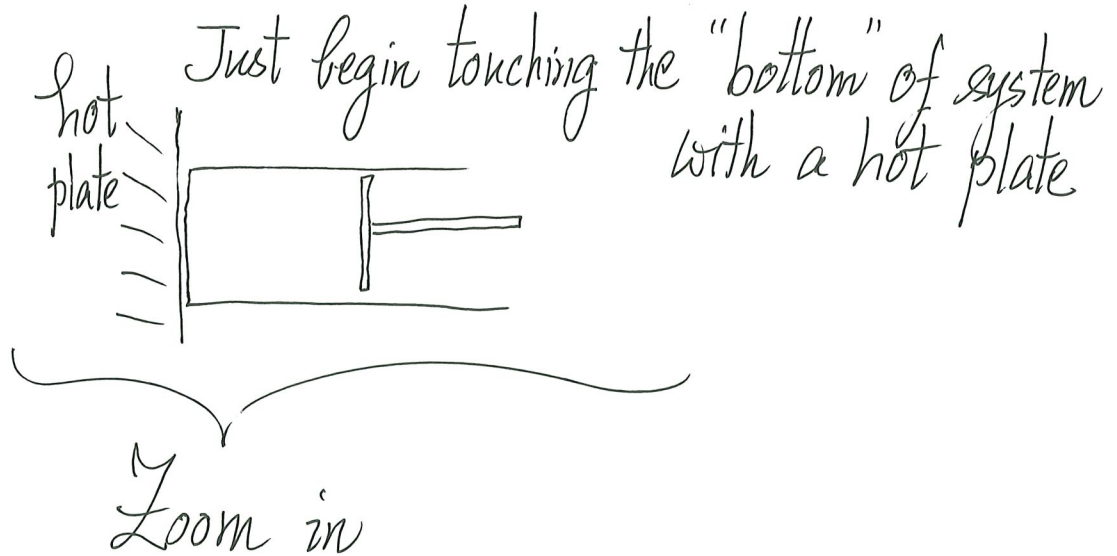
* These are thermal interaction, mechanical interaction, chemical interaction, respectively.
 All these amount to adding/subtracting ENERGY to system, that will change the STATE of system.

Equilibrium

- From experience/observations
- After something is done on a system [heat in, piston in a bit, ...] and let's wait [don't care how long it will take], system will settle into an equilibrium state



- Bulk parameters (things you can see) NOT changing in time
e.g. P , V , T , N (amount of matter)
- these state variables are uniform (the same) throughout the system
- System's equilibrium state is characterized by these (few) state variables!

fixed N 

NOT HAVING a uniform temperature in system

System is NOT in an equilibrium state
 System is OUT OF Equilibrium

We need to wait and let system to adjust to another equilibrium state

- State variables (e.g., p, V, T, N) are related through

equation of state

[ideal gas for example: $pV = NkT$]

$$pV = RT \text{ (1 mole)}$$

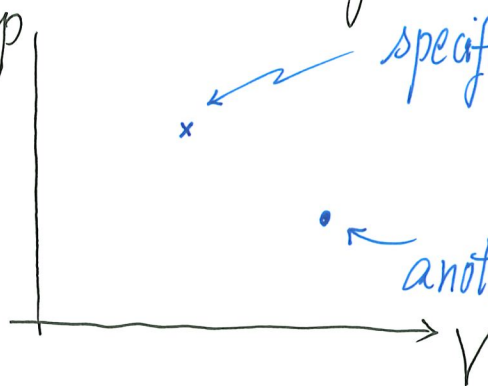
a key property of the system

⇒ Not all state variables are independent

but still free to make the choice

- State Diagram / Indicator Diagram

e.g. PV diagram



specifies (p, V) ← eg. of state gives T

thus specifies an equilibrium states

key concept!

∴ Don't have well-defined p, V, T

None equilibrium states CANNOT be dotted on to indicator diagram!

- Later, will see there are other quantities U, S, F, G, H that have a certain value depending only on the equilibrium state.
- $\begin{array}{ccc} \uparrow & \uparrow & \uparrow \\ \text{Helmholtz} & \text{Gibbs} & \text{Enthalpy} \\ \text{free energy} & \text{free energy} & \end{array}$

They are often called State Functions. In principle, p, V, T are also state functions, as their values are specified by the equilibrium state of the system. (OR $U, S, \dots$ can also be state variables.) But p, V, T were the bulk quantities easier to observe (and they helped establish the subject), they are often taken to be the state variables.

- Back to zeroth law

- Referring to systems in thermal contact

allows heat[†] in/out [no work done, no matter added]

wait → bulk properties in systems settled → equilibrium

They have a common property called Temperature.

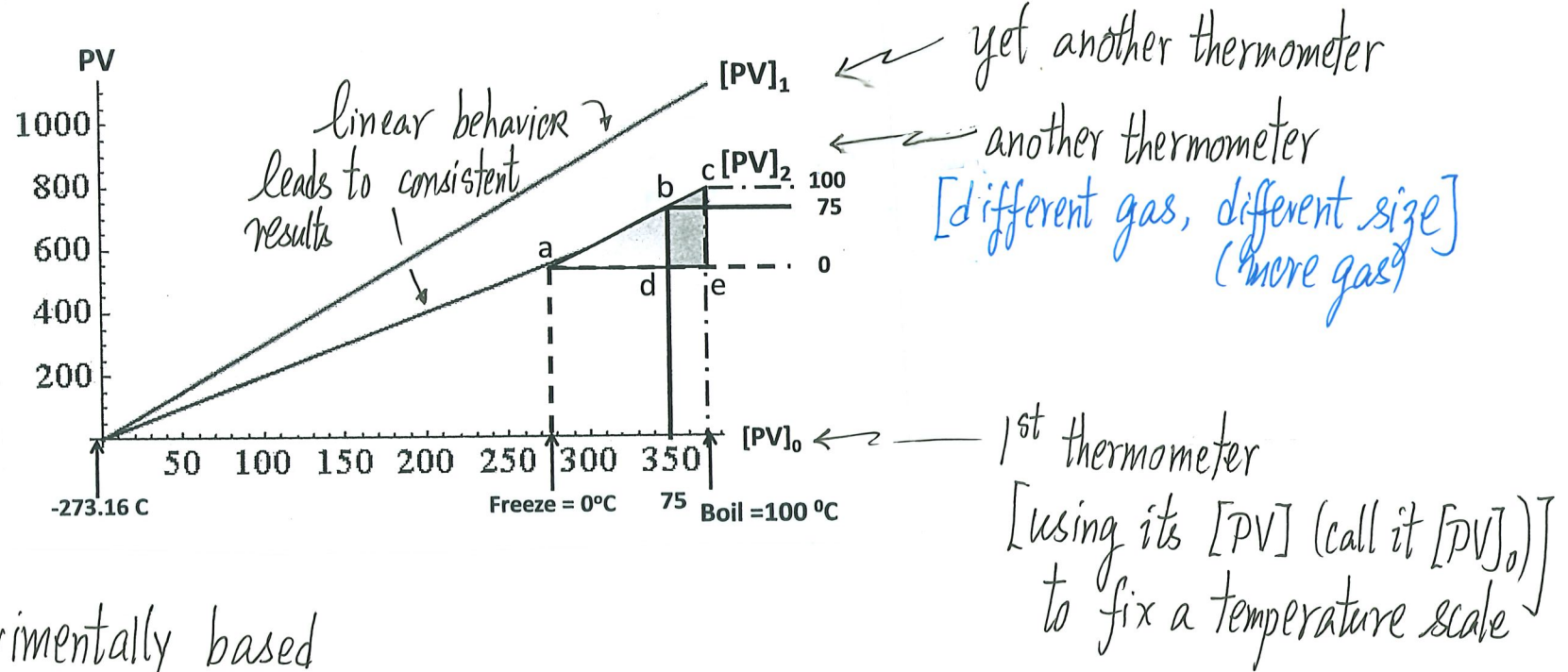
[†] Historically, heat was taken to be something unrelated to work [Newtonian mechanics]. We still use quantities such as HEAT capacities (there are tables to look up values for different materials).

A few words on Temperature Scales

- Any thing that has a property changing with hottness will do
e.g. height of mercury/alcohol in thermometers
- But will be nice to have a construction that people can follow to make a thermometer and will agree on the measurement results
- Gas Thermometers
 - Take a gas (doesn't matter which gas), calibrate $[PV]$ against selected phenomena [ice melts and water boils at sea level]
call it 0°C call it 100°C
↑—————↑
thus 100 divisions

- Follow the recipe, different thermometers will agree on the results!

Figure taken from
Shankar, "Fundamentals
of Physics I"



- experimentally based
- dilute gas [condition when different real gases behave like ideal gas]

Magical Moment in Physics

Extrapolating lines of Different Gases to low $[PV]$ (down in temperature), lines converge and meet at one point (this is the absolute zero $T = 0 \text{ K}$) [Kelvin]

▪ A rare occasion in physics!

▪ You define a measurement scale for practical reasons

hotter vs colder? at equilibrium?

▪ Then discover a behavior of NATURE

↳ there is a lowest possible⁺ temperature 0 K

[Advertisement: There is a microscopic reason (stat. mech.)]

⁺ There is No negative K.

Remarks on Systems



Isolated System

adiabatic walls

[Walls do not allow thermal, mechanical, chemical interactions with outside/surrounding]

■ Open System

Can exchange (in/out) energy (heat or work) AND matter with outside

■ Closed System in Thermodynamics

Can exchange (in/out) energy (heat or work) but NOT Matter

Remark: In Statistical Mechanics, we also use a system that can exchange heat but with fixed Volume (thus no work done) and no exchange on matter

Beyond (P, V) in (P, V, T)

- For our gas/fluid system, we have P, V specifying equilibrium state
- Other systems
 - Wire under tension [Tension $\mathcal{T}$ and extension (or length L)]
 - Paramagnetic Materials [Applied magnetic induction B_0 and total magnetic dipole moment of the system $\mathcal{M}$]
 can be magnetized by applying an external field

The Goal remains the same

- General relations among state variables, and state functions
- Stat Mech: Calculate quantities from microscopic starting point

This sets the stage for the 1st law

accounting both work and heat as Energy